

Note there is an Appendix with useful information attached to the back of the exam.
Write all your calculations and answers in the exam book.

*Appendiks med nyttig informasjon er vedlagt på baksiden av eksamensoppgaven.
Vis alle beregninger og svar i eksamensbesvarelsen.*

I. SHORT ANSWER QUESTIONS - KORTSVARSOPPGAVER

(points for each question are shown as subscripts)

(Poeng for hver oppgave er markert med senket skrift)

A. ₆ Briefly define Energy, Entropy and Exergy

₆ Definer kort begrepene energi, entropi og eksergi.

Energy is the ability to do work (kinetic + potential + mass) on an absolute scale

Entropy is a measure of the disorder of the system related to the number of possible configurations

Exergy is a measure of how far out of equilibrium *with the surroundings* that a system is, and represents the part of the energy that can be used to do work in a particular situation

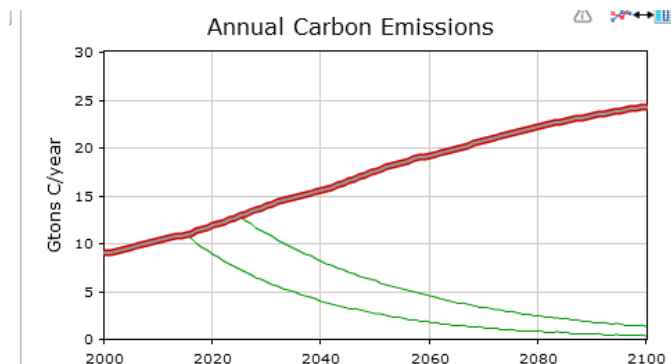
B. The graph below is from the EnRoads simulation used in the last day of class.

Grafen under er fra EnRoads-simuleringen benyttet i siste forelesning.

₄What do the green lines represent?

₄Hva representerer de grønne linjene?

The green lines are the bounds of CO₂ output allowable in the various models associated with a 2 °C increase in global temperature.



C. ₂What are the equivalents of the voltage and current when considering the case of thermal resistance of a building?

₂Hva tilsvarer spenning og strøm når en ser på termisk resistanse i en bygning?

Voltage ~ temperature difference and current ~ heat flow

D. ₃Briefly explain two problems with the use of biofuels.

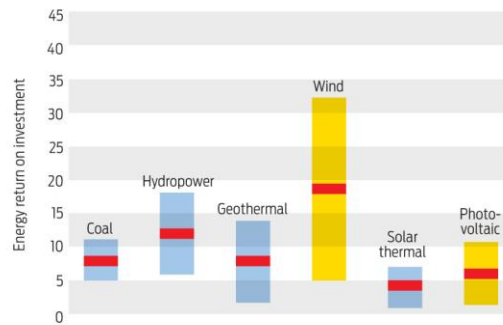
₃Beskriv kort to problemer med bruk av biodrivstoff.

Competition between food and fuel crops, land use change release of greenhouse gases, low energy density

- E. 5 Define EROI and rank two technologies from higher to lower value.

5 Definer EROI og ranger to teknologier fra høyest til lavest verdi.

Energy return on investment



- F. 4 How can the latent heat of fusion be used as part of a household energy system?

4 Hvordan kan latent smeltevarme bli brukt som del av et husholdningsenergisystem?

Using a salt that melts/freezes near a comfortable room temperature stabilizes the temperature of a thermal mass in a passive solar system, e.g. Glauber's salt.

- G. 6 What causes the electrons and holes inside a solar cell to move in opposite directions?

6 Hva er årsaken til at elektroner og hull inni en solcelle beveger seg i motsatt retning?

The transfer of charges when a p-type material contacts an n-type material leads to the formation of an internal electric field. Since electrons and holes have opposite effective charges, they move in opposite directions in the field.

II PROBLEMS - OPPGAVER

All questions should be answered.

NO CREDIT will be given for a correct numerical answer unless the work is shown!!

Alle oppgaver skal besvares.

INGEN POENG gis for riktig tallverdi hvis ikke utledning er vist!!

1. 6 Calculate the power in megawatts during outflow from a tidal power plant that encloses a rectangular area of 1.2x2.5 km, and which fills to a height of 3.7 m above the outlet. Assume an efficiency of 95%, and an emptying time of 2 hours.
6 Beregn effekten i megawatt under utstrømming i et tidevannskraftverk som dekker et rektangulært område på 1,2x2,5 km, og som fylles til en høyde av 3,7 m over utslippet. Anta 95% effektivitet og at tømning skjer over 2 timer.

$$P = \eta m g h (h/2) / t = (0.95)(1.2 \times 10^3 \text{ m})(2.4 \times 10^3 \text{ m})(3.7 \text{ m})(1.02 \times 10^3 \text{ kg/m}^3)(9.8 \text{ m/s}^2)(3.7 \text{ m}/2) / (3600 \text{ s} \times 2) = 26 \text{ MW}$$

2. 8 The production of a certain resource is increasing at 5% per year, and is predicted to be exhausted in 30 years if this continues (sudden exhaustion, no Hubbert model). A new discovery increases the total known resource by a factor of 5. How many years will it now take to exhaust the resource, assuming the growth rate remains constant?

8) Produksjonen av en gitt ressurs øker med 5% hvert år og spås tom om 30 år hvis trenden fortsetter (plutselig tømming, ingen Hubbellmodell). En ny oppdagelse øker total kjent mengde av ressurser med 5 ganger. Hvor mange år vil det nå ta før det går tomt for ressursen, hvis man antar at vekstraten forblir konstant.

$$N = N_0(1.05)^t \Rightarrow k = \ln(1.05) = 0.048$$

$$Q_T = \int_0^T N_0 e^{kt} dt = \frac{N_0}{k} (e^{kT} - 1)$$

$$5Q_T = \frac{5N_0}{k} (e^{k30} - 1)$$

$$5Q_T = \frac{N_0}{k} (e^{kt_2} - 1)$$

$$5(e^{k30} - 1) = (e^{kt_2} - 1) \quad ;$$

$$e^{kt_2} = (5 * 4.32) - 4 = 17.6$$

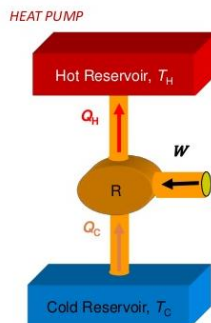
$$t_2 = 59.7 \text{ yrs}$$

3. 2A) Draw a diagram showing energy flow for a heat pump.

2A) Tegn et diagram som viser energiflyten for en varmepumpe.

6B) A particular heat pump uses 1 kW of electrical power. Every second, it removes 2.5×10^3 joules from a low temperature reservoir. What is the COP?

6B) En gitt varmepumpe har en effekt på 1 kW. Hvert sekund fjerner den $2,5 \times 10^3$ joule fra et lav-temperaturreseptat. Hva er COP for varmepumpen?



$$C.O.P. = \frac{Q_H}{Q_H - Q_C} = \frac{3.5 \text{ kW}}{3.5 \text{ kW} - 2.5 \text{ kW}} = 3.5$$

<http://www.slideshare.net/smilingsh ekhar/thermal-engineering-om>

4. 10) How much would the temperature of the earth change (and in what direction) if the albedo were increased by 1%? Assume there is no atmosphere.

10) Hvor mye ville temperaturen til Jorden endre (og i hvilken retning) hvis albedoen ble økt med 1%? Anta ingen atmosfære.

Energy absorbed by earth/area/second has to be same as radiated

$$\frac{1}{4} I_0(1-\alpha) = \varepsilon \sigma T^4$$

$$\frac{1}{4} I_0(1-\alpha_2) = \varepsilon \sigma T_2^4 \quad \text{divide}$$

$$\frac{(1-\alpha)}{(1-\alpha_2)} = \frac{T^4}{T_2^4} = \frac{.69}{.68}$$

$$T / T_2 = 1.0037$$

Temperature decreases by ~0.4 % .

(T without atm would be 254; so temperature change ~ 1K)

8The oceans contain about $1.3 \times 10^{24} \text{ cm}^3$ of water. Deuterium constitutes 0.028% by mass of natural hydrogen. 8Verdenshavene inneholder ca. $1,3 \times 10^{24} \text{ cm}^3$ vann. For naturlig hydrogen er ca. 0,028% av masen deuterium.

5.

a) What is the total energy in Joules available from this Deuterium by D-D fusion? Assume 4.0 MeV per fusion event.

a)Hva er total mengde tilgjengelig energi (i joule) fra deuteriumet ved D-D fusjon? Anta 4,0 MeV per fusjonsbegivenhet.

a)($1.3 \times 10^{24} \text{ cm}^3$)(1.02 g/cm^3)= $1.33 \times 10^{24} \text{ g H}_2\text{O}$; ~2/18 of this is hydrogen, and 2.8×10^{-4} of that is Deuterium, so $4.13 \times 10^{19} \text{ g D}$. Atomic number 2 -> each 2 grams contains 6.02×10^{23} atoms. It takes two D for each fusion event.

Energy available

($1.24 \times 10^{43} \text{ atoms} / 2(\text{atoms/fusion})$)($4 \times 10^6 \text{ eV/fusion}$)($1.6 \times 10^{-19} \text{ J/eV}$)= **$3.97 \times 10^{30} \text{ J}$**
(answers that had correct formulation without numerical values for constants received full credit)

b) For how many years could fusion reactors with 50% efficiency supply 2.0 million MW?

b)Hvor mange år kan fusjonsreaktorer med 50% effektivitet forsyne 2,0 millioner MW?

b) Reactor energy input per year = $(1/0.5) (2 \times 10^{12} \text{ J/s}) (3.15 \times 10^7 \text{ s/year}) = 1.26 \times 10^{20} \text{ J}$
(Total available)/(use per year)~ **$3 \times 10^{10} \text{ years}$** . The hard parts are extracting the D from the ocean and building the reactors...

6.5The world primary energy usage in 2013 was approximately 13 000 Mtoe.

Assuming that flat panel, non-tracking solar cells at a sunny location can harvest $8 \text{ kWh/m}^2/\text{day}$, what area is required (at that location) to supply the energy needs of the earth?

5Verdens primære energibruk i 2013 var ca. 13000 Mtoe. Anta at flate, ikke sporende solceller i et solrikt område kan produsere $8 \text{ kWh/m}^2/\text{dag}$. Hvor stort areal (i det solrike området) trengs for å forsyne verdens energibehov?

$$13000 \text{ Mtoe} = 13 \times 10^9 \text{ toe} / (8.6 \times 10^{-5} \text{ toe/kWhr}) = 1.5 \times 10^{14} \text{ kWhr/year}$$

$$(8 \text{ kWhr/day-m}^2) \times 365 = 2920 \text{ kWhr/m}^2$$

$$1.5 \times 10^{14} \text{ kWhr} / (2920 \text{ kWhr/m}^2) = \mathbf{5.2 \times 10^{10} \text{ m}^2}$$

Appendix/Vedlegg

Energy conversion factors

	J	kWh	Btu	toe
1 Joule (J)	1	2.78×10^{-7}	9.5×10^{-4}	2.38×10^{-11}
1 kilowatt-hr (kWh)	3.6×10^6	1	3413	8.6×10^{-5}
1 calorie (cal)	4.184	1.16×10^{-6}	3.97×10^{-3}	1×10^{-10}
1 British thermal unit (Btu)	1055	2.93×10^{-4}	1	2.5×10^{-8}
1 Electron volt (eV)	1.6×10^{-19}	4.45×10^{-26}	1.52×10^{-22}	3.8×10^{-30}

Equations

$$P(t) = \frac{1}{\beta} \left(1 - \frac{Q(t)}{Q_{\infty}} \right) Q(t)$$

$$Q(t) = \frac{Q_{\infty}}{1 + Ae^{-t/\beta}}$$

$$P(t) = P_0 \left(\frac{Q_{\infty}}{Q_0} \right)^2 \frac{e^{-t/\beta}}{(1 + Ae^{-t/\beta})^2}$$

$$\beta = (Q_{\infty} - Q_0) \frac{Q_0}{Q_{\infty} P_0}$$

$$t_m = \left(1 - \frac{Q_0}{Q_{\infty}} \right) \frac{Q_0}{P_0} \ln \left(\frac{Q_{\infty}}{Q_0} - 1 \right)$$

$$P_m = P(t_m) = \frac{Q_{\infty}^2 * P_0}{4Q_0(Q_{\infty} - Q_0)}$$

$$Q_T = \frac{N_0}{k} (e^{kT} - 1)$$

$$P = \frac{\Delta E}{\Delta t}$$

$$\eta = 1 - \frac{Q_L}{Q_H}$$

$$\eta_{carnot} = 1 - \frac{T_L}{T_H}$$

$$COP = \frac{Q_H}{Q_H - Q_L} = \frac{T_H}{T_H - T_L}$$

$$E = \frac{hc}{\lambda}; \quad hc = 1.98 \times 10^{-25} \text{ J} \cdot \text{m}$$

$$hc = 1.23 \times 10^{-6} \text{ eV} \cdot \text{m}$$

$$P = I^2 R$$

$$\frac{P}{A} = \sigma T^4 \quad \sigma = 5.67 \times 10^{-8} \text{ Wm}^{-2} \text{K}^{-4}$$

$$I_0 \frac{\pi R^2}{4\pi R^2} = 342 \text{ W/m}^2$$

$$\frac{1}{4} I_0 = \frac{1}{4} \alpha I_0 + I_A$$

$$\lambda_m [\mu\text{m}] = \frac{2898}{T(\text{K})}$$

$$E_{pot} = mgh = \rho Vgh$$

$$E_{kin} = \frac{1}{2} mv^2$$

$$\frac{P}{A} = 6.1 \times 10^{-4} v^3 [\text{kW/m}^2]$$

$$A = \pi r^2 = \pi \left(\frac{d}{2} \right)^2$$

$$\frac{\Delta Q}{\Delta t} = \frac{A}{R} \Delta T = AU \Delta T$$

$$R = 1/k$$

$$Q = mC\Delta T$$

$$m = \rho V$$

$$F = ma = m \frac{\Delta v}{\Delta t}$$

$$V = IR$$

$$P = 0.59 A/2(\rho u^3)$$

$$J = E * cg \sim 1 \text{ kW/m}^3 \text{ s} * T H^2$$

Storage material	MJ per kilogram	MJ per liter (litre)
Uranium-235	83 140 000[3]	1 546 000 000
Hydrogen (compressed at 70 MPa)	123	5.6
Gasoline (petrol) / Diesel	~46	~36
Propane (including LPG)	46.4	26
Fat (animal/vegetable)	37	
Coal	24	
Carbohydrates (including sugars)	17	
Protein	16.8	
Wood	16.2	

Density of water $1.02 \times 10^3 \text{ kg/m}^3$

density of air $\sim 1.2 \text{ kg/m}^3$

acceleration due to gravity 9.8 m/sec^2

Avogadro's number 6.02×10^{23} (# per mole)