Norwegian University of Science and Technology Department of Physics

EXAMINATION IN FY3201 ATMOSPHERIC PHYSICS AND CLIMATE CHANGE Faculty for Natural Sciences and Technology 26 May 2015 Time: 09:00-13:00

Number of pages: 4 Permitted help sources: 1 side of an A5 sheet with printed or handwritten formulas permitted Single or Bi-lingual dictionary permitted All calculators permitted You may take: Molar mass of water vapour: ~18 kg/kmole Molar mass of dry air: ~29 kg/kmole $N_A = 6.02 \times 10^{23}$ molecules/mole $1 \text{ hPa} = 10^2 \text{ Pa} = 10^2 \text{ N m}^{-2}$ g=9.8 m s⁻² and constant in z $273.15 \text{ K} = 0 \text{ }^{\circ}\text{C}$ Stefan–Boltzmann constant: $\sigma = 5.67 \times 10^{-8} \text{ W} \cdot \text{m}^{-2} \cdot \text{K}^{-4}$ Solar photospheric temperature, $T_s = 5786$ K Radius of the Sun = 695800 kmRadius of the Earth = 6370 km1 AU (Earth-Sun distance) = 150×10^{6} km Latent heat of vaporization water: $L_v=2.5 \times 10^6 \text{ J} \cdot \text{kg}^{-1}$ Gas constant for water vapour: $R_v=461 \text{ J}\cdot\text{K}^{-1}\cdot\text{kg}^{-1}$ Values for dry air: $C_p=1004 \text{ J}\cdot\text{K}^{-1}\cdot\text{kg}^{-1}$ $C_v=718 \text{ J}\cdot\text{K}^{-1}\cdot\text{kg}^{-1}$ $R_d=287 \text{ J}\cdot\text{K}^{-1}\cdot\text{kg}^{-1}$ $\gamma = C_p / C_v$ $\kappa = R_d / C_p$ $R_d = C_p - C_v$ $\Gamma_{da} = 9.8 \text{ K/km}$ Clausius–Clapeyron relation: $\boldsymbol{e}_s = 6.112 \, \boldsymbol{hPa} \cdot \exp\left[\frac{L_v}{R_v}\left(\frac{1}{273 \, \text{K}} - \frac{1}{T}\right)\right]$

Answer all questions (English or Norwegian). State all assumptions. Good Luck!

1) (5%) Black body radiation

Sketch the relative spectral radiance as a function of wavelength for three blackbodies at temperatures $T_1 > T_2 > T_3$. Label the curves with their temperatures and put units on the axes, but you do not need to put numerical values on the axes.

2) Multiple Choice (20%):

There is only **one** correct answer so you must **choose the best answer**. Answer A, B, C... (Capital letters), or leave the answer blank. Correct answer gives +2; incorrect answers give 0.

Write the answers for the multiple choice questions **on the answer sheet you turn in** using a table similar to the following:

Question	а	b	с	d	е	f	g	h	i	j
Answer										

a. What is the correct order of earth's atmospheric layers from bottom to top?

- A) Stratosphere, Mesosphere, Troposphere, Thermosphere, Exosphere.
- B) Stratosphere, Troposphere, Mesosphere, Thermosphere, Exosphere.
- C) Stratosphere, Troposphere, Thermosphere, Mesosphere, Exosphere.
- D) Troposphere, Mesosphere, Stratosphere, Thermosphere, Exosphere.
- E) Troposphere, Stratosphere, Mesosphere, Thermosphere, Exosphere.
- b. Which two atmospheric layers have temperature profiles that allow convection?
 - A) Mesosphere and Stratosphere.
 - B) Mesosphere and Thermosphere.
 - C) Mesosphere and Troposphere.
 - D) Stratosphere and Thermosphere.
 - E) Stratosphere and Troposphere.
 - F) None of the above.
- c. In which layer of the atmosphere is ozone the major species?
 - A) Stratosphere
 - B) Mesosphere.
 - C) Troposphere.
 - D) Thermosphere.
 - E) Exosphere.
 - F) None of the above.
- d. If the amount of energy lost by the earth to space each year were not approximately equal to that received,
 - A) The atmosphere's average temperature would change.
 - B) The length of the year would change.
 - C) The sun's output would change.
 - D) The mass of the atmosphere would change.
 - E) None of the above.

- e. From what phenomenon does the Coriolis effect arise?
 - A) Curvature of the Earth's surface.
 - B) Rotation of the spherical Earth around its axis.
 - C) Rotation of the spherical Earth around the sun.
 - D) Effect of winds high in the atmosphere.
 - E) Motion of the oceans in their basins.
 - F) None of the above
- f. Relative to the Earth's surface, what does the Coriolis effect have on masses of air or water that are changing latitude?
 - A) The results are unpredictable; currents can veer right or left in either hemisphere.
 - B) They turn to the left in the northern hemisphere and to the right in the southern hemisphere.
 - C) They turn to the right in the northern hemisphere and to the left in the southern hemisphere.
 - D) They turn to the right in both hemispheres.
 - E) They turn to the left in both hemispheres.
- g. How can we describe the scattering of sunlight by clouds?
 - A) Mie scattering theory.
 - B) Rayleigh scattering theory.
 - C) Tyndall scattering theory.
 - D) Geometric scattering theory.
 - E) None of the above.
- h. What wavelengths of sunlight are absorbed by molecular nitrogen in the troposphere?
 - A) Infrared.
 - B) Ultraviolet.
 - C) Radio waves.
 - D) Microwaves.
 - E) Visible.
 - F) None of the above.
- i. In an isothermal atmosphere, two air parcels, one wet and one dry, are continuously displaced upward. What happens to the parcel temperatures?
 - A) They remain constant since the atmosphere is isothermal.
 - B) Both parcels heat at the same rate as they get nearer to the Sun.
 - C) The wet air parcel cools faster than the dry one due to its thermal conductivity.
 - D) The dry air parcel cools faster than the wet one due to latent heat effects.
 - E) Both parcels cool at the same rate as the pressure drops.
 - F) None of the above.
- j. The geostrophic wind results from a balance between?
 - A) Coriolis force and centripetal force.
 - B) Centripetal force, pressure gradient force, and Coriolis force.
 - C) Pressure gradient force and Coriolis force.
 - D) Pressure gradient force, Coriolis force, and friction.
 - E) None of the above.

3) (25 %) Atmospheric thermodynamics, water vapour and structure

- a. A commercial airliner suffers a sudden de-pressurization due to the loss of a cargo door. If the internal and external air pressures were 850 and 350 hPa respectively, and the internal temperature was 19°C before de-pressurization, determine the final internal temperature (assume it is an adiabatic process). (5%)
- b. In practice, a fog formed in the airplane after it de-pressurized. What effect would this have on the final temperature? If the relative humidity in the cabin before it de-pressurized was 22%, how much would the final temperature change? (5%)
- **c.** In the winter hemisphere, the 500 hPa level is usually at a height of about 6000 m at a latitude of 30°, and at a height of 5600 m at a latitude of 70°. What is the mean temperature of the layer of atmosphere between 1000 hPa and 500 hPa in each case? (5%)
- d. Calculate the number density of CO₂ (365 ppmv) in the atmosphere at ground level (P = 984 hPa, $T = +18^{\circ}$ C). (5%)
- e. An air mass of temperature +10° C and pressure 1013 hPa contains 10 g/kg water vapour. Calculate the relative humidity. (5%)

4) (20%) Radiation

In another 5 $\times 10^9$ years or so, our Sun will probably become a red giant with its photospheric temperature dropping to 4000 K and its radius swelling to 3.5 $\times 10^6$ km. Under these conditions:

- a. Derive general expressions for the solar constant, S, and the effective temperature, T_e , of a planet with an albedo, α , a distance R from the sun. (6%)
- b. Calculate the solar constant and effective temperature for Earth. Earth is still 1 AU from the sun, and has an albedo $\alpha = 0.3$ (6%)
- c. What fraction of the Sun's total power output does the Earth intercept? (4%)
- d. Calculate the wavelength of maximum emission for both the Sun and Earth. (4%)

5) (30%) Greenhouse effect

The Earth's atmosphere can be modelled as an isothermal layer with temperature T_a , above the ground, which has a temperature T_g . Under normal conditions the planetary albedo, $\alpha = 0.3$, the short wavelength absorptivity of the atmosphere is $A_a = 0.21$ and the longwave atmospheric emissivity (or absorptivity) is $\varepsilon_a = 0.95$.

A large volcano erupts, creating a 2 km thick ash layer on top of the atmospheric layer, increasing the planetary albedo to $\alpha = 0.35$. The density of the ash is a constant 0.03 kg·m⁻³, and the attenuation coefficient of the volcanic ash is 0.01 m²·kg⁻¹ at all wavelengths.

- a. Sketch a diagram showing the energy exchanges between the Earth and the atmosphere. (5%)
- b. Set up the energy balance equations (9%)
 - i. at the top of the ash layer,
 - ii. at the top of the atmospheric layer,
 - iii. at the ground.
- c. Calculate the transmission of the volcanic layer (6%)
- d. Solve the energy balance equations to find the temperatures of the ash layer, T_v , the atmospheric layer, T_a , and the surface, T_g , after the eruption. (10%)