

Løsninger, Eksamen Partikkelfysikk Høst 2003

Oppgave 1.

a) En relativistisk invariant har samme verdi i alle Lorentzsystemer.

For prosess $A+B \rightarrow C+D+\dots$ er

for lab. systemet $\vec{p}_0 = 0$ og for cm. $\vec{p}_A + \vec{p}_B = 0$.

For Comptoneffekt bruker vi $\hbar = 1, c = 1$

$$p_i k_i = \text{invariant} = (E_i, \vec{p}_i) \cdot (\omega_i, -\vec{k}_i)_{\text{lab}} = (E_i, \vec{p}_i) \cdot (\omega_i, -\vec{k}_i)_{\text{cm}}$$

$$m\omega_i^2 = (E_i, \vec{p}_i) \cdot (\omega_i, -\vec{k}_i)_{\text{cm}} = \omega_i^c (E_i^c + \omega_i^c) \quad \text{og med } E_i = \sqrt{\omega_i^2 + m^2}, |\vec{p}_i| = \omega_i,$$

$$m\omega_i^2 = \omega_i^c (\sqrt{\omega_i^{c2} + m^2} + \omega_i^c).$$

b) Energi-impuls balanse $p_i + k_i = p_f + k_f$ eller

$$p_2 = p_1 + k_1 - k_2, \quad \text{kvadrering gir}$$

$$p_2^2 = p_1^2 + k_1^2 + k_2^2 + 2p_1 k_1 - 2p_1 k_2 - 2k_1 k_2$$

$$m^2 = m^2 + 0 + 0 + 2(E_1 \omega_1 - \vec{p}_1 \cdot \vec{k}_1) - 2(E_1 \omega_2 - \vec{p}_1 \cdot \vec{k}_2) - 2\omega_1 \omega_2 (1 - \cos \theta).$$

Med $\vec{p}_1 = 0, E_1 = m$ er da

$$0 = m\omega_1 - m\omega_2 - \omega_1 \omega_2 (1 - \cos \theta) \quad \text{og}$$

$$\omega_2 = \frac{m\omega_1}{m + \omega_1(1 - \cos \theta)} = \frac{\omega_1}{1 + \frac{\omega_1}{m}(1 - \cos \theta)}.$$

c) I cm. er $\vec{p}_1 + \vec{k}_1 = 0$ og $\vec{p}_2 + \vec{k}_2 = 0$ så

$$|\vec{p}_1| = |\vec{k}_1|, \quad |\vec{p}_2| = |\vec{k}_2|.$$

Energiligningen $E_1 + \omega_1 = E_2 + \omega_2$

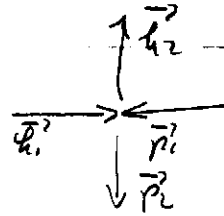
$$\sqrt{\vec{p}_1^2 + m^2} + \omega_1 = \sqrt{\vec{p}_2^2 + m^2} + \omega_2$$

$$\sqrt{\omega_1^2 + m^2} + \omega_1 = \sqrt{\omega_2^2 + m^2} + \omega_2$$

som betyr at $\omega_1 = \omega_2$ og derfor $E_1 = E_2$.

5 cm et $\theta^c = \pi/4$.

Brake ab pkr e invariant.



$$(E_1 \omega_2 - \vec{p}_1 \vec{h}_2)_{cm} = (E_1 \omega_2 - \vec{p}_1 \vec{h}_2)_L$$

$$E_1 \omega_2 - |\vec{p}_1| |\vec{h}_2| \cos \theta^c = (E_1 \omega_2 - \vec{p}_1 \vec{h}_2)_L$$

(Kannbrake hick = iuv.)

$$E_1^c \omega_2^c = m \omega_2^L$$

$$E_1^c \omega_1^c = m \frac{\omega_1^L}{1 + \frac{\omega_1^L}{m}(1 - \cos \theta^L)}$$

$$E_1^c \omega_1^c = \omega_1^c (E_1^c + \omega_1^c) / (1 + \frac{\omega_1^L}{m}(1 - \cos \theta^L))$$

$$1 + \frac{\omega_1^L}{m}(1 - \cos \theta) = (1 + \omega_1^c/E_1^c)$$

$$1 - \cos \theta = \frac{m \omega_1^c}{\omega_1^L E_1^c}$$

$$= \frac{m \omega_1^c}{\frac{\omega_1^c}{m} (E_1^c + \omega_1^c) E_1^c} = \frac{m^2}{E_1^c (E_1^c + \omega_1^c)}$$

$$\omega_1^c = m, \quad E_1^c = \sqrt{m^2 + m^2} = \sqrt{2} m$$

$$1 - \cos \theta = \frac{1}{\sqrt{2}(1 + \sqrt{2})}$$

$$\cos \theta = 1 - \frac{1}{2 + \sqrt{2}} = \frac{1 + \sqrt{2}}{2 + \sqrt{2}} = \frac{(1 + \sqrt{2})(2 - \sqrt{2})}{4 - 2} = \frac{\sqrt{2}}{2} = \frac{1}{\sqrt{2}}$$

$$\theta = 45^\circ$$

d)

5 cm, all energi gin til dæmpele av de tre massene, 3 m.

$$\omega_1^c + E_1^c = 3m$$

$$\omega_1^c + \sqrt{\omega_1^{c^2} + m^2} = 3m$$

$$(\omega_1^c - 3m)^2 = \omega_1^{c^2} + m^2$$

$$-6m \omega_1^c + 9m^2 = m^2$$

$$\omega_1^c = \frac{4}{3} m$$

for a)

$$\omega_1^L = \frac{\frac{4}{3} m}{m} (m \sqrt{\frac{16}{9} + 1} + \frac{4}{3} m) = m \frac{4}{3} \left(\frac{5}{3} + \frac{4}{3} \right) = 4m$$

Opgave 2.

c)

Partikler:

Elementare: leptoner e, μ, τ + anti

Ikke stærk v.v. Ikke S, ikke I, $m_u \neq 0$?

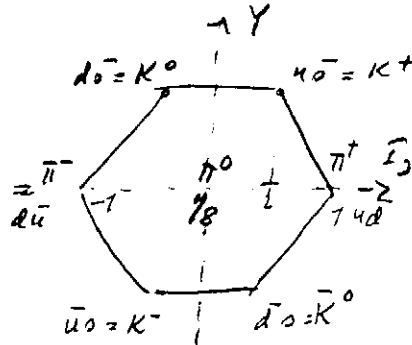
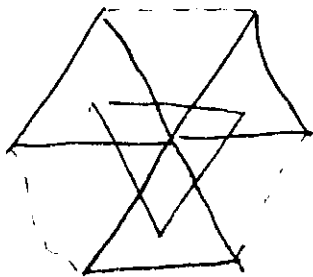
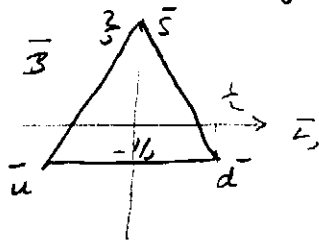
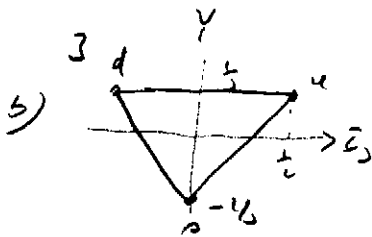
kvarkar: u, d, s, c, b, t + anti

alle v.v., fængslet. $G = \frac{1}{2}, \frac{3}{2}$, S, I, C, B, T bevar

gange partikler: $\gamma, W^\pm, Z, g$ (graviton)

el. mag, svak, sterk, (gravit) v.v. spin 2.

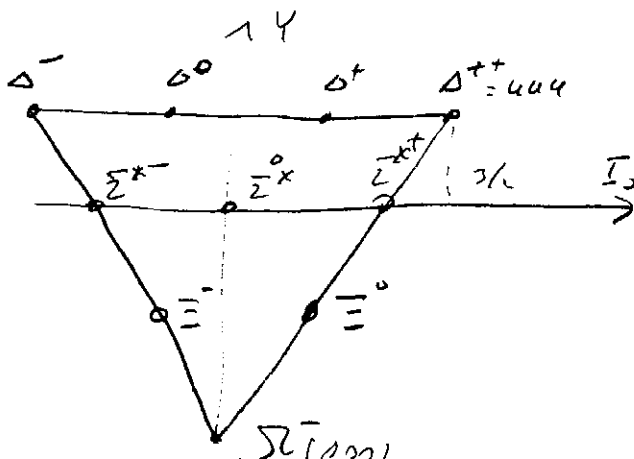
$m_g = 0, m_\gamma = 0$ fængslet, $m_u, m_t \sim 90 \text{ GeV}$.



+ γ_1

γ, γ' en lin. komb. av γ_1, γ_8 .

$$\begin{aligned} 3 \otimes 3 \otimes 3 &= \square \otimes \square \otimes \square = \square \times (\square \oplus \square) \\ &= \square \oplus \square \oplus \square + \square + \square \\ &= 10 \oplus 8 \oplus 8 \oplus 1. \end{aligned}$$



$4 \sim$ rom. spin + farge

rom. spin del en symmetrisk, antisymmetrisk + farge variable.

Oppgave 3

Θ^+ og $\bar{\Sigma}^+$ var to partikler med samme masse ladning men forskjellig deintegrasjon

$$\Theta^+ \rightarrow \pi^+ + \pi^0 \quad (2\pi)$$

$$\bar{\Sigma}^+ \rightarrow \pi^+ + \pi^+ + \pi^- \quad (3\pi)$$

Paritetsmessig

$$P_{\text{initial}} = P_{\Theta} = P_{\text{final}} = (-1)^{2\pi} (-1)^{\pi\pi} (-1)^{L_{\pi^0\pi^+}} = (-1)^{L_{\pi^0\pi^+}}$$

med $(-1)^{2\pi} = -1$. Dreieimpulsbevaring

$$\vec{J}_i = \vec{S}_{\Theta} = \vec{J}_f = \vec{S}_{\pi^0} + \vec{S}_{\pi^+} + \vec{L}_{\pi^0\pi^+} = \vec{L}_{\pi^0\pi^+} \quad \text{for } \vec{S}_{\pi} = 0, \text{ s\aa}$$

$$S_{\Theta} = L_{\pi^0\pi^+} \text{ of}$$

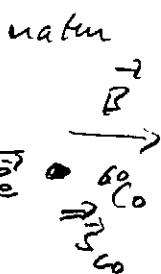
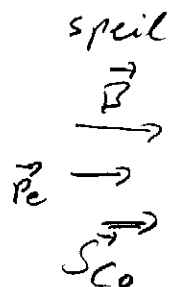
$$P_{\Theta} = (-1)^{S_{\Theta}}.$$

For $\bar{\Sigma}^+$ er

$$P_{\bar{\Sigma}} = (-1)^{2\pi} (-1)^{L_{\pi\pi}} = -(-1)^{S_{\bar{\Sigma}}}$$

s\aa enten $\Theta \neq \bar{\Sigma}$ og P bevares eller $\Theta = \bar{\Sigma}$ og P brytes.

Ekperimentelt



^{60}Co kjennet iurettes i et magnetfelt $\vec{B}$, β -elektroner utmåles retningen til.

Elektroner ut mest antiparallelt til $\vec{S}_{\text{Co}}$, ikke slik i spillbolde som altså ikke er som naturen; P brytes.

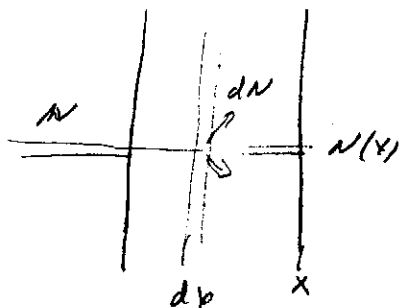
Oppgave 4

$$d\sigma = \frac{r_0^2}{2} (1 + \cos\theta) d\Omega$$

a)

$$\sigma = \int d\sigma = \frac{r_0^2}{2} \int (1 + \cos\theta) d\cos\theta d\varphi = \frac{r_0^2}{2} \cdot 2\pi \cdot (2 + \frac{2}{3}) = \frac{8\pi}{3} r_0^2$$

b)



§ dx miste vi dN

$$dN = -N \rho_s \sigma dx$$

$$\frac{dN}{N} = -\rho_s \sigma dx, \quad \kappa = \rho_s \sigma$$

$$N(x) = N_0 e^{-\rho_s \sigma x} = N_0 e^{-\kappa x}$$

$$\text{Mister } N_0 - N = N_0 (1 - e^{-\kappa x})$$

c) Intensitet halvert når $e^{-\kappa x} = \frac{1}{2} \Rightarrow x = \frac{\ln 2}{\kappa}$

For karbon i karbon:

$$x = \frac{\ln 2}{\sigma \rho_s}, \quad \sigma = \frac{8\pi}{3} r_0^2$$

ρ_s er antall elektroner pr. volumenheter

§ Ag er det N_A atomer.

§ i cm^3 er det ρ gram eller $\rho \cdot \frac{N_A}{A}$ atomer, eller

$$\rho_s = \rho \frac{N_A}{A} \approx \frac{\text{elektroner}}{\text{vol}} = 2 \cdot \frac{6.022 \cdot 10^{23}}{12} \cdot 6 \text{ el/cm}^3 = 6.022 \cdot 10^{23} \text{ el/cm}^3$$

$$x = \frac{\ln 2}{\frac{8\pi}{3} (2.179 \cdot 10^{-13})^2 \cdot 6.022 \cdot 10^{23}} \text{ cm} = \frac{0.693 \cdot 10^3}{8.32 \cdot 4.75 \cdot 6.022} \text{ cm} = 2.89 \text{ cm}$$